

1 *Cats Fishing*. Modeling The In-Game Economy

2 404 Dynamics

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# 1 Introduction

## Disclaimer:

This document may contain forward-looking statements regarding the future development and features of the Cats Fishing platform. Such statements are based on current expectations and are subject to change without notice. No reliance should be placed on these forward-looking statements as the actual outcome may differ materially due to technical, regulatory, or market factors. The \$BONE token is intended solely for in-game use and utility. It does not represent any form of equity, ownership, or investment interest in Cats Fishing or any affiliated entity. Cats Fishing does not operate an exchange, and any external trading by participants occurs solely through third-party platforms beyond the project's control. *The information in this document is provided for informational purposes only. Nothing herein constitutes legal, financial, business, or investment advice, and you should not treat any of the content as such. Cats Fishing and its token (\$BONE) are designed primarily for in-game utility and entertainment. There is no guarantee of future value, profitability or liquidity for participants. Participation may be restricted in certain jurisdictions and certain features, token distributions, or geographic availabilities described herein may be subject to change to ensure ongoing compliance with applicable laws. This document may contain forward-looking statements regarding the future development and features of the Cats Fishing platform. Such statements are based on current expectations and are subject to change without notice. No reliance should be placed on these forward-looking statements as the actual outcome may differ materially due to technical, regulatory, or market factors. The \$BONE token is intended solely for in-game use and utility. It does not represent any form of equity, ownership, or investment interest in Cats Fishing or any affiliated entity. Cats Fishing does not operate an exchange, and any external trading by participants occurs solely through third-party platforms beyond the project's control. We are actively monitoring applicable laws and regulations and are committed to adhering to applicable legal frameworks. However, players are responsible for understanding and complying with the laws of their respective jurisdictions when participating in the Cats Fishing game.*

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61 *ownership, or investment interest in Cats Fishing or any affiliated entity. Cats*  
62 *Fishing does not operate an exchange, and any external trading by participants*  
63 *occurs solely through third-party platforms beyond the project’s control.*

64 *Cats Fishing* is a multiplayer fishing game, where anyone can go fishing on  
65 several virtual islands, collect and build exciting items, and meet new friends.  
66 Inspired by successful games such as Animal Crossing, the game combines the  
67 best of both worlds—a fun narrative for regular players who want to enjoy the  
68 gameplay experience, as well as a blockchain-enabled in-game economy for those  
69 who enjoy collecting NFTs.

70  
71 The game is aimed at a diverse gaming community and can be easily accessed  
72 from regular platforms. Our main comparison lies within the traditional gaming  
73 market with the same core audience. We are innovating an unobtrusive way of  
74 connecting an exciting game narrative to blockchain features. *Cats Fishing has the*  
75 *potential to attract a large community of gamers, providing an engaging in-game*  
76 *economy that rewards player skill, creativity, and strategic decision-making. All*  
77 *references to ‘rewards’ refer solely to in-game items, tokens, or other progression*  
78 *benefits.*

79  
80 In this document, we focus on describing the models and mechanisms for  
81 the in-game economy of *Cats Fishing*. As discussed later, this involves various  
82 protocols and computations designed to keep gameplay both fun and balanced.  
83 Our ultimate goal is to design in-game mechanisms that are enjoyable for all types  
84 of players, while striving for a robust in-game economic design that maintains  
85 the integrity of the gaming experience over speculative interests.

## 86 1.1 Why this?

87 **Disclaimer** *While Cats Fishing draws on lessons from previous Web3 games, we are*  
88 *committed to working within applicable legal frameworks. Mechanisms described*  
89 *here are intended to enhance gameplay and user experience, not to encourage*  
90 *speculative trading.*

91 The design of token economics in gaming ecosystems represents a critical  
92 frontier in the evolution of digital entertainment and virtual economies. Indeed,  
93 while blockchain gaming promises to revolutionize player ownership and value  
94 creation, historical evidence demonstrates both the potential and pitfalls of token-  
95 based gaming economies. Traditionally, one could argue that Web3 as a whole has  
96 been rather driven by short-term profitability (e.g., having users *dumping* their

97 token shortly after they're received), however, this is a behavior that mechanism  
98 designers can attempt to correct by introducing sufficiently robust incentives to  
99 behave in a desired way. As such, the success of these systems hinges on careful  
100 economic design that prioritizes sustainable player engagement over short-term  
101 speculation.

102  
103 Indeed, early attempts at gaming *tokenomics*, such as *Axie Infinity*'s [Tea21]  
104 initial model, highlighted the vulnerabilities of yield-focused designs. During its  
105 peak in 2021, Axie Infinity achieved a market capitalization exceeding \$8 billion,  
106 with over 2.7 million daily active users [XHWZ24]. However, the ecosystem's  
107 heavy reliance on continuous player growth and unsustainable yield mechanisms  
108 led to a significant market correction, demonstrating the importance of balanced  
109 economic design.

110  
111 In contrast, more sustainable models have emerged from platforms that priori-  
112 tize gameplay experience while incorporating token mechanics as complemen-  
113 tary features. Analysis of successful blockchain games reveals that sustainable  
114 token economies require careful balance between value accrual and value cre-  
115 ation mechanisms [XCGM22]. These findings from empirical studies of early  
116 blockchain games suggest that token economics must be designed as an extension  
117 of compelling gameplay rather than as the primary driver of player engagement.

118  
119 For Cats Fishing, these lessons emphasize the importance of designing token  
120 mechanics that enhance the core fishing and collection mechanics while avoiding  
121 the common pitfalls of over-financialization. The game's focus on accessibility  
122 and traditional gaming audiences aligns with successful approaches observed in  
123 the market, where blockchain features serve to augment rather than define the  
124 player experience [RS23].

125  
126 This white paper outlines our approach to creating a balanced token economy  
127 that supports both casual players and engaged collectors<sup>1</sup> while maintaining  
128 long-term sustainability. Through careful mechanism design and targeted utility  
129 functions, we aim to demonstrate how blockchain technology can enhance rather  
130 than disrupt traditional gaming experiences.

---

<sup>1</sup>Engagement here is to be understood solely in terms of in-game progression and enjoyment

## 1.2 Core Mechanics

*Cats Fishing* combines three core systems: *fishing game play*, *item collection & management*, and an *in-game economy* based on the game’s native currency: the \$BONE token. All of these systems are designed with sustainable and robust token economics in mind. Players engage with these systems through their cat characters, making strategic decisions about catching, storing, and trading fish while managing resources and progression. Each system is carefully balanced to create engaging gameplay loops that reward the player’s loyalty to the game. In this subsection, we will explore these components in more detail.

**Game Play** The core mechanism of the game is fairly simple: Cats go and fish, and when they catch something, they can either take it to the marketplace to sell the fish, or to the restaurant/fish monger to have it cooked. Naturally, cats need to eat, otherwise their Health Points (HP) will decrease; however, in *Whiskery Woods*, cats can’t eat raw fish – it needs to be cooked. Thus, whenever a cat catches a fish, they need to decide whether they want to sell it or eat it. It is worth mentioning that players can catch and store multiple fishes at any given point. The HP management system serves as a crucial economic stabilizer by creating consistent token demand through necessary gameplay activities. Players must regularly purchase cooked fish from restaurants using \$BONE tokens to maintain their HP levels, which are consumed during fishing activities. The HP consumption rate increases with more advanced fishing activities, creating a natural balance between earning potential and maintenance costs. This system helps maintain token velocity while preventing excessive accumulation by requiring regular expenditure for continued participation.

**Remark.** *While \$BONE may be used in third-party marketplaces or traded between players, Cats Fishing does not operate any such external exchange or provide guarantees regarding liquidity or pricing.*

**Token Economy** The token is supported through multiple interconnected economic mechanisms. On the supply side, sophisticated algorithms manage resource availability through dynamic adjustment of catch rates and population regeneration. The catching rate  $\mu_I(t)$  responds to current fish populations and player activity levels, creating natural scarcity when needed while ensuring sufficient resources for active gameplay. This is complemented by the birth process  $\lambda_I(t)$ , which manages resource regeneration based on current population levels

166 and carrying capacity. This is discussed in more detail in Section 3.

167

168 Fish prices follow carefully designed pricing functions that incorporate both  
169 exponential and constant elasticity models. These functions respond to supply  
170 levels and market conditions, ensuring that prices in \$BONE tokens accurately  
171 reflect resource scarcity while maintaining economic stability. The pricing model  
172 includes parameters for both immediate market conditions and longer-term  
173 trends, creating a balanced and predictable economic environment. This is  
174 further discussed in Section 4.

175 **Item Collection and Management** The equipment progression system forms  
176 a central pillar of token utility. Here, players begin with basic fishing gear and  
177 progressively upgrade their equipment using \$BONE tokens earned through  
178 gameplay. Each tier of equipment unlocks new fishing capabilities, access to  
179 more valuable fish species, or improved efficiency in existing activities. This  
180 progression system is carefully balanced to ensure that investments in better  
181 equipment translate to proportionally improved earning potential, maintaining  
182 the value proposition at each tier of progression.

183

184 The marketplace serves as a means for player to e.g., buy their fish, as well  
185 as equipment, in-game items, etc. All in-game marketplace activities occur in  
186 \$BONE tokens, creating a closed economic loop that maintains token utility.  
187 The marketplace incorporates sophisticated pricing mechanisms that account  
188 for multiple variables including supply levels, item rarity, and market demand.  
189 Special items and rare catches can be tokenized as NFTs, adding another layer of  
190 value and trading opportunities within the ecosystem. Economic Value Drivers.

### 191 1.3 Organization

192 The rest of this document is structured as follows. In Section 2 we outline the  
193 core components of the token economy. Here, we begin by mapping the key  
194 stakeholders, and discuss the key value drivers of the economy. In Section ??, we  
195 present a potential distribution mechanism for the \$BONE token. In Section 3  
196 we present the proposed mechanism for how fishes are caught and appear in the  
197 game, and in Section 4, we discuss how these fishes are priced within the game.  
198 As we will see, both of these mechanisms will in turn depend on several "global"  
199 parameters, such as the number of players, their activity, etc. Lastly, in Section 5,  
200 we discuss how players can level up in the game, and why they are incentivized

201 to do so. The rest of the in-game documentation can be found in [Tea24].

## 202 **2 The \$BONE Token Economy**

203 The *Cats Fishing* economy is built around the \$BONE token, which serves as the  
204 primary in-game medium of exchange within the platform’s ecosystem. This  
205 section outlines the token’s purpose, its utility in gameplay, and the mechanisms  
206 designed to support long-term stability and player engagement. We begin by  
207 describing the main stakeholders in the *Cats Fishing* economy.

### 208 **2.1 Token Use Cases and Economic Flows**

209 The \$BONE token underpins *Cats Fishing*’s various economic interactions, weav-  
210 ing together player actions, resource management, and in-game progression.  
211 Below, we discuss its key uses and the core economic flows that sustain player  
212 engagement.

#### 213 **2.1.1 Resource Generation and Primary Economic Activities**

214 The fundamental economic activity within *Cats Fishing* centers around the fish-  
215 ing mechanic, where players engage with the game’s primary resource generation  
216 system. Players participate in fishing activities that require skill, strategy, and  
217 resource management. Each fishing expedition presents opportunities to catch  
218 various species of fish, with different varieties holding distinct values based on  
219 their rarity, attributes, and current market conditions.

220  
221 The fishing system incorporates sophisticated mechanics that consider mul-  
222 tiple factors including player skill, equipment quality, location selection, and  
223 timing. More skilled players who invest in better equipment and develop effi-  
224 cient strategies can access higher-value fishing opportunities, creating a natural  
225 progression system that rewards dedication and strategic thinking. This core  
226 gameplay loop establishes the foundation for all subsequent economic activities  
227 within the ecosystem.

#### 228 **2.1.2 Token Earning Mechanisms**

229 Players earn \$BONE primarily by selling their catches to **in-game restaurants**.  
230 These restaurants apply dynamic pricing algorithms that adjust based on supply-  
231 demand conditions inside the game. Ideally, each such in-game transaction is

232 subject to some nominal fee (a percentage  $\varphi_{\text{restaurants}}$  of the traded amount). This  
233 amount would then go to the game treasury. Once in the treasury the community  
234 could decide, via standard governance mechanisms, what to do with these tokens  
235 (e.g., burn them, use them for ecosystem development, etc).

236  
237 Fish pricing follows sophisticated formulas that incorporate both immediate  
238 market conditions and longer-term trends. When certain fish species become  
239 scarce due to increased catching activity, their value in \$BONE tokens automat-  
240 ically adjusts upward, creating natural market dynamics that reward strategic  
241 resource gathering. Conversely, abundant fish species may see price decreases,  
242 encouraging players to diversify their fishing activities and maintain ecosystem  
243 balance.

244  
245 Notice that while players may earn \$BONE through gameplay, these mechanics  
246 are designed solely for in-game engagement and utility. \$BONE is not intended  
247 to hold monetary value or generate real-world financial returns

### 248 2.1.3 Token Expenditure Systems

249 To keep the in-game economy dynamic and stable, *Cats Fishing* implements  
250 multiple “token sinks” that encourage ongoing spending of \$BONE . The result  
251 is a balanced cycle of earning and spending.

252 **Equipment and Progression System** The equipment marketplace represents  
253 a primary token sink within the economy. Players can upgrade from basic rods  
254 to advanced gear, opening up more efficient or rewarding fishing opportunities.  
255 Players can upgrade from basic rods to advanced gear, opening up more efficient  
256 or rewarding fishing opportunities. Higher-tier equipment is priced in \$BONE  
257 , creating a natural loop where earned tokens are spent to improve gameplay,  
258 rather than idle or speculate. Ideally, these transactions should also subject to  
259 some nominal fee (a percentage  $\varphi_{\text{equipment}}$  of the traded amount). This amount  
260 wold then go to the game treasury.

261  
262 **Health Point (HP) Management** The HP system serves as another crucial  
263 token sink, creating consistent demand through necessary gameplay mainte-  
264 nance activities. Players must manage their characters’ HP levels by purchasing  
265 prepared fish dishes from restaurants using \$BONE tokens. This mechanic intro-



266 duces a strategic element to resource management, as players must balance their  
267 earnings between progression investments and sustained gameplay activities.

268  
269 The HP consumption rate scales with activity level and fishing location dif-  
270 ficulty, creating a natural balance between earning potential and maintenance  
271 costs. More challenging fishing activities that offer higher rewards also typically  
272 require greater HP investment, maintaining the risk-reward ratio across different  
273 player segments.

274 **Economic Feedback Loops** The interaction between these various systems  
275 creates multiple reinforcing feedback loops that drive sustained economic activ-  
276 ity. When players invest in better equipment, they gain access to more profitable  
277 fishing opportunities. These increased earnings can then be reinvested in further  
278 equipment upgrades or used for HP maintenance, creating a sustainable cycle of  
279 economic activity.

280  
281 This feedback system is carefully balanced to ensure that investments in  
282 progression provide meaningful returns while maintaining overall economic  
283 stability. The relationship between investment costs and potential returns is  
284 continuously monitored and adjusted through sophisticated algorithms that  
285 consider multiple economic indicators including catch rates, token velocity, and  
286 market prices.

287 **Market Dynamics and Price Discovery** All these economic activities con-  
288 tribute to natural price discovery mechanisms within the ecosystem. The constant  
289 flow of tokens between earning and spending activities, combined with dynamic  
290 pricing algorithms, ensures that token value reflects true market conditions  
291 while maintaining stability. The system implements various economic controls  
292 to prevent market manipulation and ensure sustainable value creation. These  
293 include rate limiting on certain activities, dynamic pricing adjustments based on  
294 volume, and sophisticated monitoring systems that track key economic indica-  
295 tors. Through these mechanisms, the economy maintains balanced token flows  
296 while providing clear value propositions for all participants.

297  
298 Through this comprehensive system of economic activities, the \$BONE token  
299 establishes itself as both a medium of exchange and a store of value within  
300 the Cats Fishing ecosystem. The careful balance between token sources and  
301 sinks, combined with sophisticated price discovery mechanisms and progression

302 systems, creates a sustainable economic environment that rewards strategic  
303 gameplay while maintaining long-term stability.  
304

## 305 2.2 Value Accrual Mechanisms

306 The design of value accrual mechanisms in *Cats Fishing* is focused on ensuring a  
307 self-sustaining and engaging in-game economy. These mechanisms are intended  
308 to balance gameplay progression with the utility of the \$BONE token. The to-  
309 ken’s value is derived solely from its continuous use within the game, thereby  
310 reinforcing player engagement and overall ecosystem stability.  
311

312 One key component is the transaction-based in-game value mechanism. Every  
313 transaction made **within the game**—whether it involves purchasing equipment,  
314 in-game objects, or cooked fish incurs a small fee. These fees will, in principle  
315 go to the in-game treasury, where their use may be determined by governance  
316 mechanisms as they develop. A portion of the fees is allocated to periodic token  
317 burns, which create a deflationary pressure by reducing the overall token supply,  
318 while another portion is dedicated to funding ongoing improvements and special  
319 community events. The objective of this mechanism is to enhance the quality of  
320 the gameplay experience by ensuring that tokens continuously circulate within  
321 the ecosystem.  
322

323 Another important component is the integration of staking and governance  
324 features. Players who opt to stake their \$BONE tokens unlock a range of in-  
325 game benefits such as reduced transaction fees, priority access to new fishing  
326 areas, and exclusive equipment options. In addition, staked tokens confer limited  
327 governance rights that allow players to participate in decisions affecting certain  
328 game parameters, including adjustments to fishing rates or the scheduling of  
329 community-driven events. It is important to emphasize that these governance  
330 rights are strictly confined to in-game and ecosystem-related matters and do not  
331 grant any ownership, dividend, or profit-sharing rights in the underlying project.  
332

333 The game also employs adaptive economic controls to maintain long-term  
334 stability. The system continuously monitors key metrics such as fish populations,  
335 player activity, and token velocity. In response to fluctuations in these metrics,  
336 the game automatically adjusts supply-side elements like resource regeneration  
337 rates and applies dynamic pricing models for in-game goods. Advanced machine  
learning algorithms are integrated into this process to predict potential imbal-

ances and to recommend preemptive adjustments. These adaptive measures are designed to ensure that the in-game economy remains balanced and engaging, even as external conditions evolve.

These mechanisms are designed exclusively to promote in-game utility and an engaging player experience. While these mechanisms support the stability and continuous development of the in-game economy, they do not provide any assurance of real-world financial returns or profit-sharing. All benefits associated with the \$BONE token are intended solely to enhance gameplay and community interactions within the *Cats Fishing* ecosystem.

### 3 Catching the Fish

In *Cats Fishing*, the probability of a successful catch depends on a complex interplay of three fundamental categories: *Environmental Conditions*, *Cat Characteristics*, and *Fish Properties*. These parameters interact through different correlation mechanisms that determine fishing success. Environmental factors form the foundation of fishing mechanics. Each location (Whisker Woods, PawHaven, Purr Harbor, Catnip Cove, and Norway) provides unique fishing conditions. Water properties, temperature, wind conditions, weather patterns, and time of day all influence fishing success through various correlation mechanisms.

A cat's capabilities significantly impact fishing success through several key attributes: location access, experience level, fishing technique proficiency, and premium status benefits. The inventory system, including rods, rigs, tools, and consumables, provides additional layers of strategic depth through equipment-based modifiers. Fish characteristics determine both their availability and catch difficulty. These include rarity tier (Common, Rare, Trophy), preferred fishing method compatibility, movement patterns, bait preferences, and hook size requirements. Each parameter creates specific conditions that must be met for successful catches.

The fishing success mechanism is modeled as a Poisson process for theoretical analysis, transitioning to a Bernoulli process in practical implementation. The probability of  $k$  fish biting within a time interval  $\tau$  is given by:

$$\Pr(X = k; \tau, \mathbb{P}, \Lambda, \mathbb{W}) = \prod_{p \in \mathbb{P}} \mathbb{I}_p(v) \times \frac{(\lambda_\Lambda \cdot \tau)^k}{k!} \exp(-\lambda_\Lambda \cdot \tau) \quad (1)$$

Where  $\lambda_\Lambda$  aggregates all influencing parameters:

$$\lambda_\Lambda = \lambda_0 + \sum_{p \in \Lambda_+} w_p \lambda_p + \sum_{p \in \Lambda_-} w_p \lambda_p \quad (2)$$

### 3.1 Implementation Considerations

While the theoretical model uses continuous time, the actual game implementation discretizes time into fixed intervals (typically 5-10 seconds). This transforms the Poisson process into a Bernoulli process, where each interval presents a chance for a successful catch. The probability of success in each interval is derived from the Poisson rate through:

$$p = \frac{\lambda_\Lambda \cdot \tau}{n} \quad (3)$$

This implementation provides a balanced compromise between mathematical accuracy and computational efficiency while maintaining engaging gameplay mechanics.

## 4 Pricing the Fish

In this section we present our dynamic pricing methodology for the fishes in the game. We begin by formally describing some properties for the fish in the game. These properties will later play a central role in the remaining supply of fish. We can consider each *fish* as a tuple  $F$  containing (at least) the following properties:

- $l \in \mathbb{N}$  : The level of the fish,
- $\ell_{\min} \in \mathbb{N}$ : The minimum level that a player needs to have in order to start catching this fish,
- $k \in \mathbb{N}$ : The class of fish, where, in general there can be  $K$  different classes of fish in the game.

- 391 •  $t \in \mathbb{R}_{\geq 0}$  : Time the fish was caught,
- 392 •  $\phi : \mathbb{R}_{\geq 0} \rightarrow [0, 1]$  : The freshness of the fish (i.e., how long ago it was
- 393 caught). Here  $\phi(t)$  is a decreasing function of  $t$  such that  $\phi(t) = 0 \forall t \geq t^*$ ,
- 394 for some arbitrary *spoilage time*  $t^*$
- 395 •  $\rho \in [0, 1]$ : The *rarity* of the fish (color, weight, attributes, etc)

396 For a given fish  $f$ , we will refer to these properties as  $f_P$ , where  $P = \{l, \ell_{\min}, k, t, \dots\}$   
 397 denotes the set of properties. Our design will be based on the following guiding  
 398 decisions.

399 GD. 1 *The price of any fish depends on its attributes. Thus, in equilibrium and all*  
 400 *else being equal, higher level, rarer, fresher fish should have a higher price.*

401 GD. 2 *Spoiled fish (i.e., fish having  $\phi(t) = 0$ ) have a price of 0.*

402 GD. 3 *The game has shared, finite resources. In particular, this means that players*  
 403 *compete to catch the same fish.*

404 As the game evolves, players will go and catch fish either to sell or to eat.  
 405 Given that the game has shared resources, we need to design a *supply chain* of  
 406 fishes that reacts to the amount of fish being caught. While we can't *directly*  
 407 control the amount of fish being caught (as this will depend on several factors,  
 408 such as the number of players in the game, etc), we can model it, and propose a  
 409 *replenishing* mechanism that reacts to this demand accordingly.

## 410 4.1 Modeling demand

411 Consider a specific group of fish characterized by the tuple  $I = (\ell, \ell_{\min}, k)$ , and  
 412 let  $N_I(t)$  denote the number of fish of type  $I$  at time  $t$ . Furthermore, assume that  
 413 at any given time  $t$  there are  $N_\ell^u(t)$  users at level  $\ell$ . This means that these users  
 414 will be able to catch any fish  $f$  such that  $\ell \geq f_{\ell_{\min}}$ .

415 Players catch fish at random times, decreasing the fish population. The *catching*  
 416 *rate*,  $\mu_I(t)$  for fish of type  $I$  at time  $t$  is proportional to both the fish population  
 417 and the number of players that can catch these fish, i.e.,

$$\mu_I(t) = c_I(t) \cdot N_I(t) \cdot N_\ell^u(t) \quad (4)$$

418 where  $c_I(t) \geq 0$  is the *catchability coefficient* — an **unknown** parameter related  
 419 to the scarcity of the fish since higher  $c_I$  implies a lower population of the fish.

420 In practice, this rate  $\mu_I(t)$  can be estimated by taking a sample average on a time  
 421 window  $\Delta t$

$$\mu_I(t) \approx \hat{\mu}_I(t) = \frac{\text{Number of fish caught in a window } \Delta t}{\Delta t} \quad (5)$$

422 Which in turn implies that rate  $c_I(t)$  can also be estimated as follows:

$$c_I(t) \approx \hat{c}_I(t) = \frac{\hat{\mu}_I(t)}{N_I(t)N_t^u(t)} \quad (6)$$

423 Estimating such a parameter will be useful later in our formulation.

## 424 4.2 Supply mechanism

425 Notice that if we assume that fishes do not regenerate at a given rate, then,  
 426 eventually, the fishes of group I will go extinct. Naturally, this is something that  
 427 we want to avoid — otherwise it would ruin the UX for newer players. To that  
 428 end, we present a model for how fishes *regenerate* in the game. In particular, we  
 429 propose that fish regenerate according to some time-dependent random process.  
 430 This is to avoid predictability of the game over time.

431 We propose to implement a *birth process* for the replenishing of fish. Loosely  
 432 speaking, this means that fish of type I will replenish at a rate of  $\lambda_I(t)$ ; that is, on  
 433 average, we propose that there are  $\lambda_I(t)$  new fishes per unit of time. Specifically,  
 434 here we propose setting  $\lambda_I(t)$

$$\lambda_I(t) = r_I(t) \cdot N_I(t) \left( 1 - \frac{N_I(t)}{N_{I,\max}(t)} \right) N_t^u \quad (7)$$

435 where  $r_I(t)$  is the intrinsic growth rate of type I at time t, and  $N_{I,\max}$  is the  
 436 so-called *carrying capacity* of fishes of type I, i.e., the maximum number of this  
 437 kind of fish that can be in the environment at any given time. The core idea here  
 438 is to algorithmically adjust  $r_t, N_{I,\max}$  so that there's some sort of balance between  
 439 the amount of available vs caught fish at any time.

## 440 4.3 Ensuring sustainability

441 To maintain a sustainable fish population and a positive user experience, we  
 442 must carefully choose the supply parameters so that, adaptively,

$$\frac{d\mathbb{E}[N_I(t)]}{dt} = \lambda_I(t) - \mu_I(t) = 0 \quad (8)$$

443 Notice that here we are taking the expected value since, in practice, the catching  
 444 rate, and the amount of fishes left is a random process depending on the amount  
 445 of players and the activity of the game. **More concretely**, our goal is to adjust  $r_t$   
 446 and  $N_{I,\max}$  to maintain a stable fish population  $N_I(t)$ , despite fluctuations in the  
 447 death rate due to player activity.

448 Substituting the expressions for  $\lambda_I(t)$  and  $\mu_I(t)$ :

$$r_I(t) \cdot N_I(t) \left(1 - \frac{N_I(t)}{N_{I,\max}}\right) N_t^u = c_I(t) \cdot N_I(t) \cdot N_{t,t}^u$$

449 Simplify by dividing both sides by  $N_I(t)$  (assuming  $N_I(t) > 0$ ):

$$r_I(t) \left(1 - \frac{N_I(t)}{N_{I,\max}}\right) = c_I(t)$$

450 solving for  $r_I(t)$  yields

$$r_I(t) = \frac{c_I(t)}{1 - \frac{N_I(t)}{N_{I,\max}}} \quad (9)$$

451 Lastly, notice that in practice, we don't know  $c_I(t)$ , but can estimate it adap-  
 452 tively using Equation (3) above, which in turn results in an estimate to be used  
 453 in Equation (5).

#### 454 4.4 Pricing as a function of supply

455 Given the dynamic supply management described above, we can simply propose  
 456 a price of a given fish of class  $I$ , in terms of BONEs as

$$P_I(t) = f_I(N_I(t), \epsilon) \cdot (\text{add ons}) \quad (10)$$

457 where  $f_I : \mathbb{N} \times \mathbb{R}_{>0} \rightarrow \mathbb{R}_{>0}$  is a predetermined pricing function for this specific  
 458 class of fish,  $\epsilon > 0$  is a parameter related to the price elasticity of supply and the  
 459 term *add ons*  $> 0$  corresponds to multiple add-ons that affect the price (either  
 460 positively or negatively), based on its freshness, rarity, etc. There are several  
 461 potential choices of  $f_I$ , e.g.,

$$\begin{aligned} \text{Exponential:} \quad & P_I(t) = ae^{-\epsilon N(t)} \\ \text{Constant Elasticity:} \quad & P_I(t) = bN(t)^{-\epsilon} \end{aligned}$$

These are illustrated in Figure 1. While the final version of  $P_I(t)$  will be discussed in a further document, *a priori* we believe that the exponential might prove itself better suited for rapid changes in the game.

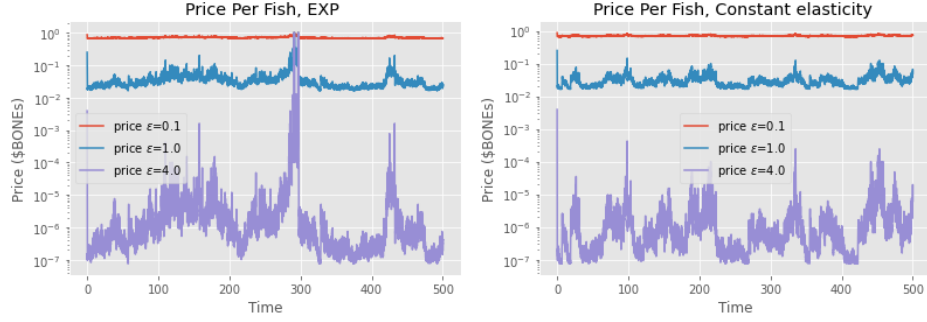


Figure 1. Price elasticity

## 5 Leveling up

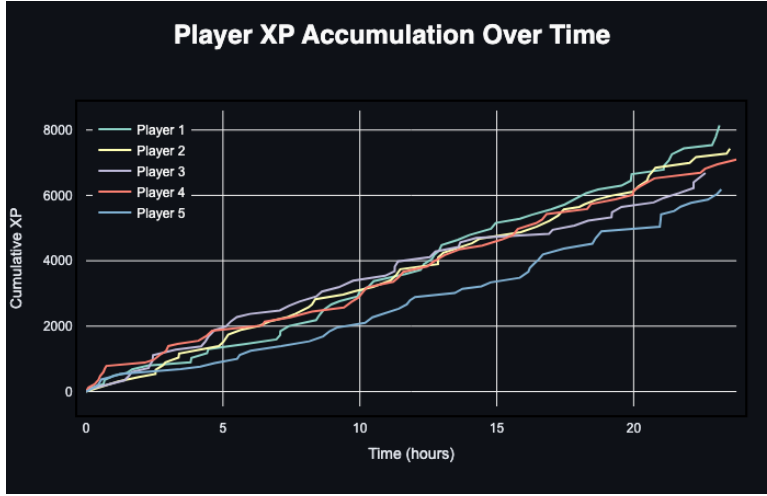
The experience (XP) system in Cats Fishing serves as the core progression mechanism, carefully designed to maintain player engagement while supporting the game’s tokenomics. In particular, level systems in games should obey an *effort-benefit analysis*; this is the case of, e.g., Role Playing Games, where higher level characters are stronger or have otherwise better developed attributes. In the specific case of *Cats Fishing*, the motivation behind leveling up is simple: **as players increase their level, they are able to use better equipment and catch increasingly rarer and more valuable fish**. In what follows, we present a comprehensive mathematical framework that governs player advancement and its implications for game design.

For a game with  $K \in \mathbb{N}$  distinct fish types, each player  $u$  accumulates experience through successful catches. The total experience gained from each catch incorporates multiple strategic factors. Let  $XP_{\text{base},i}$  represent the base experience for fish type  $i$ , which is then modified by equipment quality, player level, and fish characteristics. Given this, the fundamental XP calculation is given by:

$$XP_{\text{total},i}^u = XP_{\text{base},i} \prod_{j \in \text{Multipliers}} M_{j,i}^u \quad (11)$$

where  $M_{j,i}^u \in \mathbb{R}_{>0}$  corresponds to the multiplier given to a user  $u$  due to factor  $j$  when catching some fish  $i$ . These factors include, e.g., equipment bonus, level,





**Figure 2.** Example XP accumulation

484 how fresh the fish is, the specific type of fish caught, etc. Here, base XP values  
 485 should be set proportional to fish rarity and market value:

$$\text{XP}_{\text{base},i} = \alpha \times \text{rarity}_i + \beta \times \text{market value}_i, \quad \alpha, \beta \in \mathbb{R}_{>0}, \quad (12)$$

486 where rarer fish can only be caught by players with a higher level (and which,  
 487 all else being equal, have a higher market value).

488 Thus, the cumulative XP for a player who has caught  $N_u \in \mathbb{N}$  fish during their  
 489 whole gameplay is expressed as:

$$\text{XP}_{\text{current}}^u = \sum_{i=1}^{N_u} \text{XP}_{\text{total},i}^u. \quad (13)$$

490 This is illustrated in Figure 2.

491 We consider two primary approaches for level progression thresholds:

$$\text{Exponential: } \text{XP}_{\text{required}}^{\text{exp}}(\ell) = A \cdot B^{C \cdot \ell} \quad (14)$$

$$\text{Polynomial: } \text{XP}_{\text{required}}^{\text{poly}}(\ell) = \sum_{i=0}^M a_i \cdot \ell^i \quad (15)$$

492 For some constants  $A, B, C, M > 0$  and  $\{a_i\}_{i=0}^M$  chosen so that  $\text{XP}_{\text{required}}^{(\cdot)}(\ell) > 0$   
 493  $\forall \ell \geq 0$ . Notice that one can also create a (potentially piecewise) combination of  
 494 these two.

Based on game design principles and tokenomic considerations, we recommend implementing a polynomial progression system with dynamic difficulty scaling. The progression function should be:

$$\text{XP}_{\text{required}}(\ell) = A \times \ell^B \times D(t) \quad (16)$$

where  $D(t)$  is a Dynamic Difficulty Modifier (DDM) based on server-wide progression metrics at time  $t$ . The concept of a DDM has deep roots in game design. Games like *Half-Life 2* and *Left 4 Dead* pioneered these systems through their AI Director, which continuously adjusts challenge levels based on player performance. In the MMO space, *World of Warcraft* has refined this approach over multiple expansions, implementing various catch-up mechanics that help new players join endgame content more efficiently as the game matures. For *Cats Fishing*, the idea is to implement a similar DDM of the form

$$D(t) = \alpha' \times \left(1 + \beta' \times \left(\frac{\ell_{\text{avg}}(t)}{\ell_{\text{target}}(t)} - 1\right)\right) \times \left(1 + \gamma \times \left(\frac{N_{\text{active}}(t)}{N_{\text{base}}} - 1\right)\right) \quad (17)$$

In this setting, when players progress faster than intended (that is, when average level exceeds target level), the XP requirements gradually increase to maintain game longevity and economic balance. The system also responds to player population changes – as the player base grows beyond baseline expectations, requirements adjust slightly to prevent economic inflation, similar to *EVE Online*’s resource spawn rate adjustments. Conversely, if average levels fall behind target or player counts drop, the requirements decrease, creating natural catch-up mechanics for new or returning players.

The implementation draws inspiration from several successful games. *Guild Wars 2*’s dynamic events system adjusts difficulty based on participant count and success rates, while *Path of Exile* regularly tunes its progression rates based on league performance data. *Final Fantasy XIV* implements experience bonuses for classes below the average level, creating natural catch-up mechanics that maintain healthy player distribution.

**Remark.** The implementation parameters  $(\alpha, \beta, \gamma \in \mathbb{R})$  can be fine-tuned as player data becomes available.

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